

On the New Branch of Mathematical Science-Part 2

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Abstract: The fifth Euclidean postulate problem in geometry is 2300 years old. This postulate is well known as Euclid's parallel postulate. The great mathematicians tried to deduce the fifth postulate from the other four postulates. But unfortunately nobody could succeed in this geometrical battle. The studies devoted to this problem led to the origin of two non-Euclidean geometries. The authors resurveyed and established and gave a proof for this problem.

Key words: Euclid, elements, postulates, non-Euclidean geometries, physical applications

INTRODUCTION

Construction: Construct two congruent Lambert quadrilaterals as shown in Fig. 1. In Fig. 1, $AB = FE$, $BC = CF$, CD is common. The angles at A, B, C, F and E are right angles.

In this research, we do not assume Euclid's fifth postulate.

quadrilaterals $ABCM$ and $EFCM$ are congruent. So, angles M, CMA, CME and FEM are equal. Since angle $B = 90^\circ$, angle MAM is obtuse. i.e., x is obtuse. So, angle AME is more than 180° . Now AM is extended up to R . From this we get that $\angle ARE < 90^\circ$. This is a contradiction. So, in Lambert quadrilateral $ABCD$, side CD cannot be smaller than AB .

METHODS AND MATERIALS

In this study we begin where Saccheri attempted to obtain the result. In this study the application of number theory, matrix algebra, set theory and quadratic, cubic and quadric equations may be used.

RESULTS

Case 1: In a Lambert quadrilateral $ABCD$, if we assume that sides AB and CD are equal, then it is a Saccheri quadrilateral. Saccheri showed that the summit angles in his quadrilateral are equal. Since the angle at A is 90° , the angle at D is also 90° . This establishes Euclid's parallel postulate. Proving the fifth Euclidean postulate from the other four postulates is not merely difficult but impossible. So, AB and CD cannot be equal.

Case 2: Let us assume that CD is smaller than AB . On the extension of CD , make $CM = AB$. Join AM and EM . Now by SASAS correspondence, Saccheri

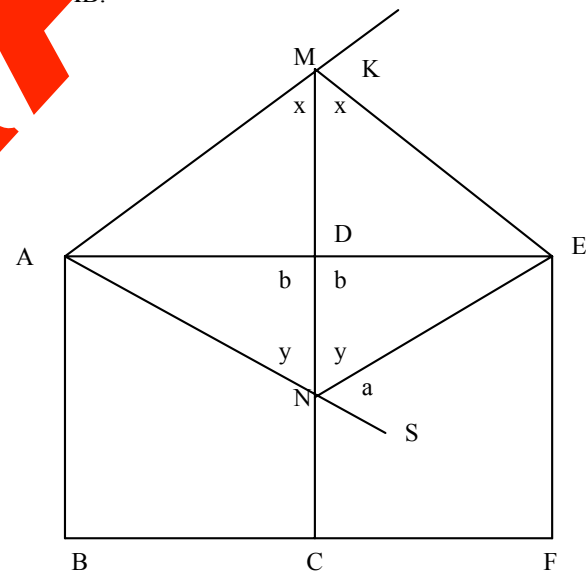


Fig. 1: Euclidean

Case 3: Let us assume CD is greater than AB . On CD , make $CN = AB$. Join AN and EN . As we have seen in case 2, Saccheri quadrilaterals $ABCN$ and $EFCN$ are

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congruent. So, the angles BAN, CAN, CNE and FEN are equal. Since the angle BAD is 90° , angle BAN is acute. So, the angles CAN and CNE are equal and acute. Since angle CAN is acute, angle AND is obtuse. So, $2y$ is more than 180° . Now extend AN up to S. Here $2y+a = 180^\circ$. This is also a contradiction So, our assumption that CD is greater than AB is not acceptable.

DISCUSSION

From cases 1 2 and 3 we get that in Lambert quadrilateral ABCD, the lateral sides AB and CD is neither greater, nor smaller or equal. This is a peculiar geometrical phenomenon. Why is so? Where is the mystery? It is up to interested researchers to probe into this problem and unlock the hidden treasure which will definitely give birth to a new field of mathematical science. If AD and CD are equal, consequently this establishes the fifth Euclidean postulate which is impossible to prove.^[1, 2, 3, 4]

CONCLUSION

Labachevsky, the noted Russian mathematician, the first person in the history of mathematics to formulate a model of non-Euclidean geometry which is also known as hyperbolic geometry. The formulae of this branch of geometry are widely used to study the properties of atomic objects in quantum physics. Also, the celebrated German mathematicians Gauss and Riemann developed the second branch of non-Euclidean geometry which is known as elliptic geometry. Einstein is using the concepts of

Riemannian geometry nearly took 10 years to formulate his general theory of relativity. The authors do not make any top claim but politely state that the result is consistent. There is a hidden treasure. Further studies will definitely unlock this problematic problem and definitely give birth to a new branch of mathematics. The turning point in geometry is also a milestone in physics. Modern physics is facing many open problems. The new future field will solve some physical problems such as monopoles, quantum gravity, the properties of electrons of an atom, dark matter, dark energy, the nature of matter, gravitons and black holes.

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